

**Déjà****1 (homogeneous) sample:** "Survival" / "Time-to-event" data:

- [equivalent] Functions:  $S[t]$  , hazard  $h[t]$  , pdf $[t]$
- Links: e.g.  $S[t] = \exp[-\int_0^t h[u] du]$ , integral from u=0 to u=t
- Summaries of these functions (e.g.  $T_{25}$ ,  $T_{50}$ ,  $S[T]$ )
- *Non-Parametric / Semi-Parametric Estimation*  
(point & interval) of  $S[t]$  ,  $h[t]$  and pdf $[t]$   
--- Lifetable [fixed-] --- K-M [data-determined intervals]
- *Censored data not necessarily "time - to - event"*  
 $Y = \text{PSA levels} < \text{detection limit}$ , salaries in intervals, distance travelled on set of tires, pages on single ink cartridge, etc.
- *Not covered, but possible: Parametric models\**

**Comparison of 2 Survival/Hazard Curves or Distributions**

- Risk Sets
- Adjusted comparisons (non-regression methods)
- *Not covered, but possible: Parametric models\**

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\* The **SAS LIFEREG** procedure fits parametric models to failure time data that can be right, left, or interval censored. The models for the response variable consist of a linear effect composed of the covariates and a random disturbance term. The distribution of the random disturbance can be taken from a class of distributions that includes the extreme value, normal, logistic, and, by using a log transformation, the exponential, Weibull, lognormal, loglogistic, and gamma distributions.

**Stata streg** performs maximum likelihood estimation of parametric regression survival-time models. Survival models currently supported are exponential, Weibull, Gompertz, lognormal, log-logistic and generalized gamma. Also see help stcox for estimation of proportional hazards models.

**New****Regression Models (semiparametric)**

- Model (event) *rates* or *hazards* p h reg
- Models are multiplicative in rates/hazards  
linear predictors if work in log[rate] or log[hazard] scale
- Proportionality of rates or hazards p h reg  
Constancy of rate ratio parameter over time-bands
- Avoid modelling the nuisance parts  
don't fit parameters that (a) are not our focus (b) waste "d.f."
- Use risksets & conditioning to reduce # parameters
- Choice of Time-scale and "Time-zero" is important  
(has implications for risksets)
- Models, and conditioning as a way of eliminating parameters, applicable to matched case-control studies and even to c-c and other (e.g. consumer choice\*) studies with no 'time' element  
(\* Daniel McFadden shared the Nobel Prize for his development of theory and methods for analyzing discrete choice in Economics:  
<http://www.nobel.se/economics/laureates/2000/mcfadden-autobio.html>)

**Readings** (\* = 3 most relevant for now, to be handed out in class 08/03)

[ <http://www.epi.mcgill.ca/hanley/c681/cox> ]

- \* Clayton&Hills, Ch 22 Intro to regression models
- \* Pair of expository articles by JH
- \* Clayton&Hills, Ch 30 Cox's Method, specifically...  
pp 298; bottom of pp 300 to top of p 304; Exercise 30.1

**Data:** Framingham Study

[ <http://www.epi.mcgill.ca/hanley/c681/cox> ]

**Other Resources**

- **Texts** [<http://www.epi.mcgill.ca/hanley/c681/cox>]  
Kleinbaum's 'Self-Learning' textbook, Chapter 3  
Collett Textbook, Chapter 3  
Hosmer & Lemeshow's Applied Survival Analysis

.... TIME Scale = YEAR\_of\_research\_grant ...

**TIME Scale = AGE** . (NOTE how delayed entry is specified)

Testing Global Null Hypothesis: BETA=0

-2LOGL W/out: 24098.1 With: 23968.1 Covariates: Chi-Sq(1) 130; p=0.0001

## Maximum Likelihood Estimates

|          |    | Parameter | Standard | Wald   | Pr >   | Risk  |
|----------|----|-----------|----------|--------|--------|-------|
| Variable | DF | Estimate  | Error    | Chi-Sq | Chi-Sq | Ratio |
| I_MALE   | 1  | 0.583     | 0.051    | 129.3  | 0.0001 | 1.79  |

Testing Global Null Hypothesis: BETA=0

-2LOGL W/out:22819.8 With:22662.7 Covariates; Chi-Sq(1) 157; p=0.0001

## Maximum Likelihood Estimates

|          |    | Parameter | Standard | Wald   | Pr >   | Risk  |
|----------|----|-----------|----------|--------|--------|-------|
| Variable | DF | Estimate  | Error    | Chi-Sq | Chi-Sq | Ratio |
| I_MALE   | 1  | 0.643     | 0.051    | 156.3  | 0.0001 | 1.90  |